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STABILITY AND CONTROL FORCE TESTS OF FOUR- AND

SIX-UNIT WING DESIGNS OF LOW ASPECT

RATIO AND 20° TRIANGULAR PLAN FORM

By John W. Paulson, Joseph L. Johnson,
and Elizabeth P. Varney

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NACA

WASHINGTON

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SUMMARY

An investigation has been made to obtain force-test
data on a wing design suitable for high-speed guided
missiles, particularly data on rolling moments produced
in yawed and pitched attitudes. Force tests were con-
ducted on two models of a wing design of low aspect
ratio and 20° triangular plan form. One model consisted
of four wings spaced 90° and the other consisted of six
wings spaced 60°.

Results of the tests showed that appreciable rolling
moments existed for both the four- and six-unit wing
designs in yawed and pitched attitudes but that the
rolling moments of the six-unit design were considerably
smaller than those of the four-unit design. The values
of these moments, which became larger as the angles of
attack and yaw were increased, were attributed to partial
blanketing of one or more wings by the other wings.
Fairly large control deflections were required to trim
out the rolling moments produced in the climbing-turn
attitudes.

INTRODUCTION

The analysis presented in reference 1 indicates
that compressibility effects are delayed by the use of
low-aspect-ratio wings of triangular plan form. In con-
nection with the design of such a wing arrangement
suitable for use on high-speed guided missiles, the
rolling-moment characteristics in yawed and pitched
attitudes have been determined.

Force tests were conducted in the Langley free-flight tunnel on two models of the design. One model consisted of four wings spaced 90° and the other consisted of six wings, identical to those of the first model, spaced 60°. Tests were made for a range of angle of attack from 0° to 20° with the models set at an angle of yaw of 0° but rotated in roll about the body axes by 10° increments from one symmetrical condition to the next. Thus, the first model was rotated through 90° and the second was rotated through 60°. In this manner, conditions of sideslip and angle of attack that would be attained in climbing turns were simulated. Particular attention was given to any evidence of rolling moments in these attitudes.

SYMBOLS

C_L lift coefficient $\left(\dfrac{\text{Lift}}{qS}\right)$

C_D drag coefficient $\left(\dfrac{\text{Drag}}{qS}\right)$

C_Y lateral-force coefficient $\left(\dfrac{\text{Lateral force}}{qS}\right)$

C_m pitching-moment coefficient $\left(\dfrac{\text{Pitching moment}}{qbS}\right)$

C_n yawing-moment coefficient $\left(\dfrac{\text{Yawing moment}}{qbS}\right)$

C_l rolling-moment coefficient $\left(\dfrac{\text{Rolling moment}}{qbS}\right)$

q dynamic pressure $\left(\dfrac{1}{2}\rho V^2\right)$

ρ air density, slugs per cubic foot

V airspeed, feet per second

S wing area, square feet (2.82)

b   wing span, feet (1.41)

L   rolling moment

N   yawing moment

M   pitching moment

α angle of attack, degrees

β angle of sideslip, degrees

ϕ angle of roll, degrees

ψ angle of yaw, degrees

δ_{a_R} right-aileron deflection, degrees

δ_e elevator deflection

δ_r rudder deflection

APPARATUS AND MODELS

The force tests were made in the Langley free-flight tunnel with the models mounted on the six-component balance described in reference 2. The models used in the investigation were of triangular plan form with an included angle of 20^0 and an aspect ratio of about 0.7. The models were made of spruce with each unit of constant thickness except for the leading edge, which was shaped to an elliptical section. Drawings of the four- and six-unit wing models are presented as figure 1. Photographs of the models showing the brackets used to mount the models on the balance strut are shown as figures 2 and 3. These brackets were used to minimize the interference effects of the strut.

For a few tests the four-unit wing model was modified by the installation of a control surface at the trailing edge of one wing. This modification was accomplished by installing a $2\frac{1}{2}$-inch-chord flap. (See fig. 1.)

TESTS

All force tests were made at a dynamic pressure of
4.1 pounds per square foot, which corresponds to an air-
speed of about 40 miles per hour and to a test Reynolds
number of 510,000 based on an average chord of 2 feet.
Tests were made over a range of angle of attack from 0°
to 20° with the models rotated by 10° increments from 0°
to 90° for the four-unit wing model and from 0° to 60°
for the six-unit wing model.

All coefficients are based on a wing area of
2.82 square feet and a wing span of 1.41 feet and are
referred to the stability axes (which are identical with
the wind axes in the present case because all tests were
made at an angle of yaw of 0°) originating 2.67 feet
from the apex. The stability axes are a system of axes
in which the Z-axis is in the plane of symmetry, perpen-
dicular to the relative wind and directed downward; the
X-axis is in the plane of symmetry, perpendicular to
the Z-axis and directed forward; and the Y-axis is perpen-
dicular to the plane of symmetry and directed to the
right. A sketch of the stability axes is presented as
figure 4. Arrows indicate the positive direction of
moments, forces, and control-surface deflections.

RESULTS AND DISCUSSION

Application of Results

The angles of attack and sideslip simulated by each
test condition can be determined from the test data by
using the following relationships:

$$\alpha_{simulated} = \alpha \cos \phi \tag{1}$$

$$\beta_{simulated} = \alpha \sin \phi \tag{2}$$

Dividing equation (2) by equation (1) gives

$$\frac{\beta_{simulated}}{\alpha_{simulated}} = \tan \phi$$

Similarly, the lift and lateral-force coefficients pro-
duced by the angles of attack and sideslip simulated
in each test condition can be obtained from the lift-
coefficient test data by using the following relation-
ships:

$$C_{L_{simulated}} = C_L \cos \phi$$

$$C_{Y_{simulated}} = C_L \sin \phi$$

Any lateral-force coefficients measured in the force
tests (for which $\beta = 0^\circ$) are evidence of additional
lift and lateral force that are probably caused by
partial blanketing of one or two of the wings by the
other wings. These additional lift and lateral-force
coefficients can be obtained from the lateral-force
data by using the following relationships:

$$\Delta C_{L_{simulated}} = C_Y \sin \phi$$

$$\Delta C_{Y_{simulated}} = C_Y \cos \phi$$

Four-Unit Wing Design

The force-test data for the four-unit wing design
are presented in figure 5 and crossplots of these data
against angle of roll are presented in figure 6. The
values of C_Y, C_n, and C_l presented in these figures
are incremental values taken between an angle of roll
of $0°$ and each succeeding angle of roll. The results in
figure 5 show that the slope of the pitching-moment curve
increased with increasing angle of attack. At the same
time, however, the lift-curve slope increased so that
the aerodynamic center did not move appreciably with
increasing angle of attack. The increase in lift-curve
slope with increasing angle of attack is in agreement
with results of tests of low-aspect-ratio wings presented
in reference 3.

The data of figures 5 and 6 show that for angles of
attack of $5°$ and $10°$ no appreciable variation occurred in
lift, drag, or pitching-moment coefficients with angle
of roll. For angles of attack of $20°$, however, the coef-
ficients did vary with angle of roll and were lowest at
angles of roll of about $40°$ or $50°$ - that is, when the
simulated angles of attack and sideslip were about the
same magnitude.

The results in figures 5 and 6 also show that
appreciable rolling moments, yawing moments, and lateral
force were measured in the force tests and varied with
angle of roll and angle of attack. These forces and
moments are shown in figure 6 to be approximately zero
at the symmetrical conditions of angles of roll of $0°$,
$45°$, and $90°$. At intermediate angles of roll, however,
forces and moments were produced that reached a maximum
at angles of roll of about $20°$ and $65°$ and that increased
with angle of attack. Since the forces and moments are
smallest for the symmetrical conditions, the variation
of forces and moments is attributed to partial blanketing
of one or more wings by the other wings as the model
simulated various angles of yaw and pitch.

The data show that in a simulated straight pull-up,
a flat turn, or a climbing turn represented by the con-
dition in which the angle of roll is $45°$, no lateral
force was introduced. For any of the intermediate
conditions, however, a lateral force was produced that
would cause the missile to deviate from its path, and

additional control would therefore be required to maintain
the desired path. In a similar manner, the rolling
moments produced in the various climbing-turn attitudes
must be balanced by the use of aileron control.

The results of tests made to determine the effective-
ness of a control surface installed on one wing of the
four-unit design are presented in figure 7. These data
show that a small control deflection (less than 10°) in
the zero-roll condition produced a larger rolling moment
at high angles of attack than at low angles of attack.
The results of tests made to determine the effect of
blanketing on the control effectiveness are also pre-
sented in figure 7 and show a slight decrease in the
rolling moment produced by control deflection when the
control was on the downwind side.

Six-Unit Wing Design

The results of the force tests of the six-unit wing
design are presented in figure 8 and crossplots of the
data against angle of roll are presented in figure 9.
The lateral data are also incremental values as in the
case of the four-unit wing design. The results in fig-
ure 8 show that the pitching-moment curve of the six-unit
design had characteristics similar to those of the
pitching-moment curve for the four-unit design. Figure 8
also shows that the lift curve remained approximately
straight throughout the angle-of-attack range. At low
angles of attack the lift-curve slope for the six-unit
design is about 50 percent greater than that for the
four-unit design because the six-unit design has 50 per-
cent more effective lifting-surface area. At the higher
angles of attack, however, this increase in lift was not
realized, probably because of additional interference
effects. The data of figures 8 and 9 show very little
variation of the lift, drag, and pitching-moment coef-
ficients with angle of roll for angles of attack of 5°
and 10°. For an angle of attack of 20°, however, the
lift and pitching-moment coefficients varied considerably
and were lowest at angles of roll of 0° and 60°, whereas
the drag coefficient remained nearly constant. These
variations are attributed to interference effects, as in
the case of the four-unit design.

The results presented in figures 8 and 9 show the
same general variation of rolling-moment, yawing-moment,
and lateral-force coefficients for the six-unit design
in the simulated climbing-turn conditions as for the four-
unit design, although the variation was not so systematic
and the maximum values of the forces and moments were not
so large as those of the four-unit design. Although
aileron and rudder control would be needed to trim out
the forces and moments for the six-unit design, the deflec-
tions required would be considerably less than for the
four-unit design.

CONCLUDING REMARKS

Stability and control force tests of four- and six-
unit wing designs of low aspect ratio and 20° triangular
plan form have been made in the Langley free-flight
tunnel. From the results of the tests, appreciable rolling
moments were found to exist for both the four- and six-
unit wing designs in yawed and pitched attitudes but
the rolling moments of the six-unit design were consider-
ably smaller than those of the four-unit design. The
values of the unsymmetrical forces and moments, which
became larger as the angles of attack and yaw were increased,
were attributed to partial blanketing of one or more wings
by the other wings. Fairly large control deflections
were required to trim out the rolling moments produced
in the climbing-turn attitudes.

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REFERENCES

1. Jones, Robert T.: Properties of Low-Aspect-Ratio
     Pointed Wings at Speeds below and above the Speed
     of Sound. NACA TN No. 1032, 1946.

2. Shortal, Joseph A., and Draper, John W.: Free-Flight-
     Tunnel Investigation of the Effect of the Fuselage
     Length and the Aspect Ratio and Size of the Vertical
     Tail on Lateral Stability and Control. NACA ARR
     No. 3D17, 1943.

3. Zimmerman, C. H.: Characteristics of Clark Y Air-
     foils of Small Aspect Ratios. NACA Rep. No. 431,
     1932.

A-A

Four-unit wing

$2\frac{1}{2}''$

4'

Six-unit wing

$16\frac{15}{16}''$

90°

60°
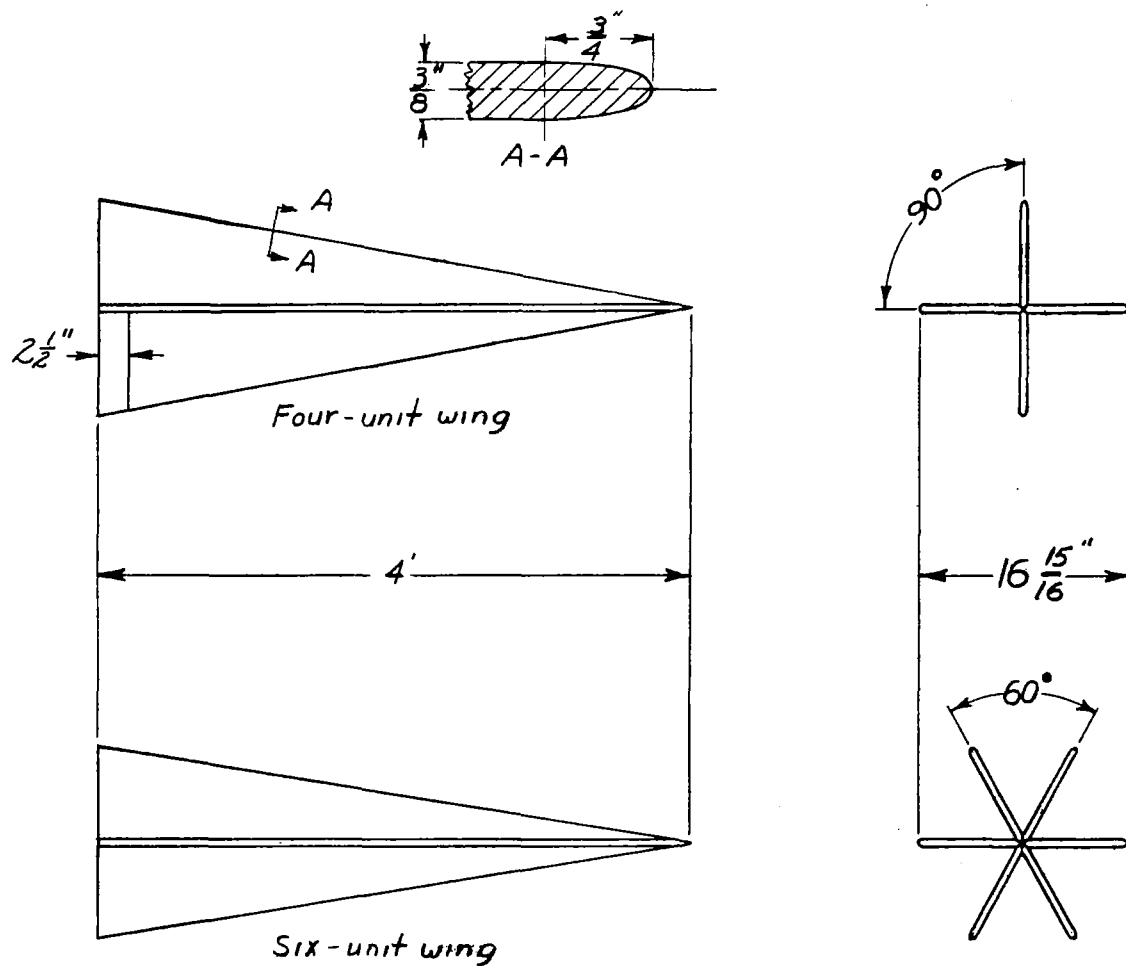
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Figure 1.- Four- and six-unit wing designs of low aspect ratio and triangular plan form for guided missiles tested in the Langley free-flight tunnel.

Fig. 1
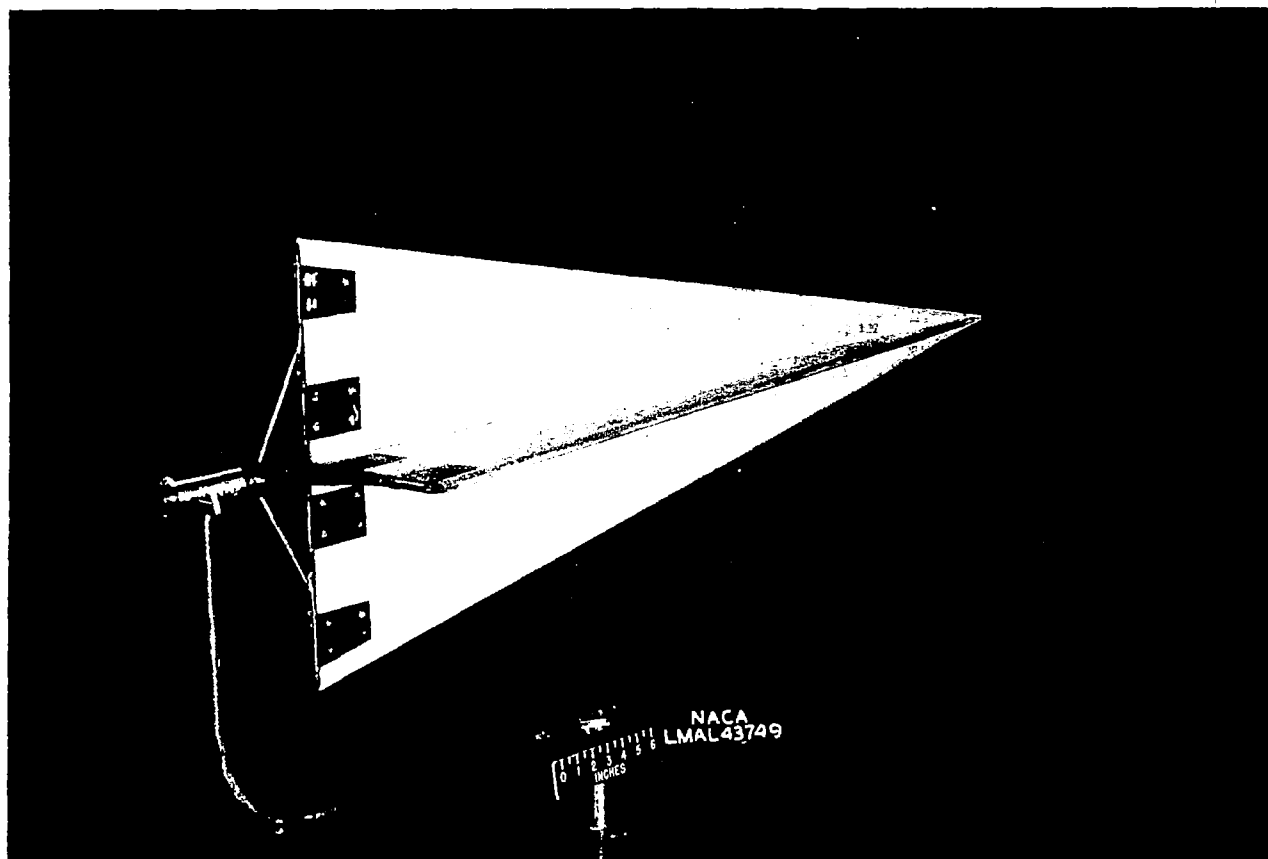
(a) $\phi = 0^{\circ}$.

Figure 2.- Model of four-unit wing design of low aspect
ratio and triangular plan form for guided missiles
tested in the Langley free-flight tunnel.

NACA
LMA_43752
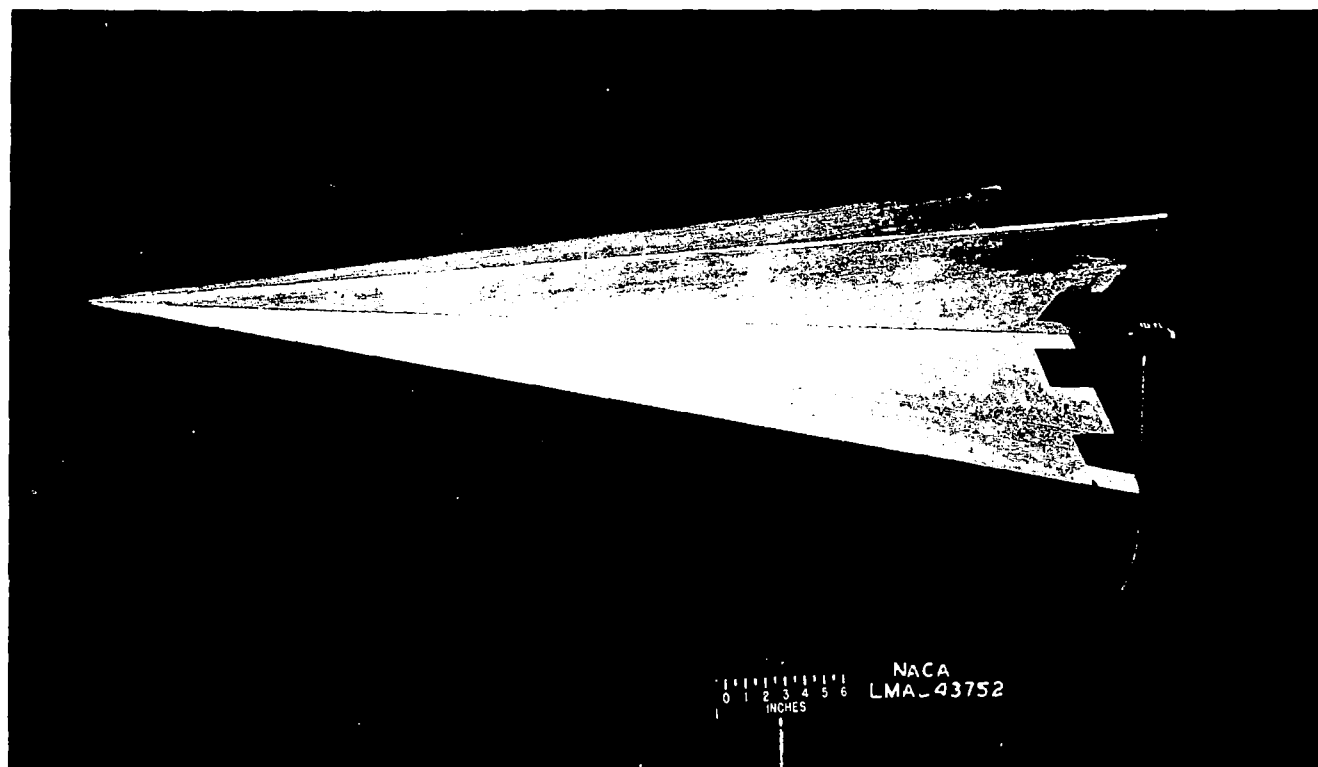
(b) $\phi = 40^\circ$.

Figure 2.- Concluded.
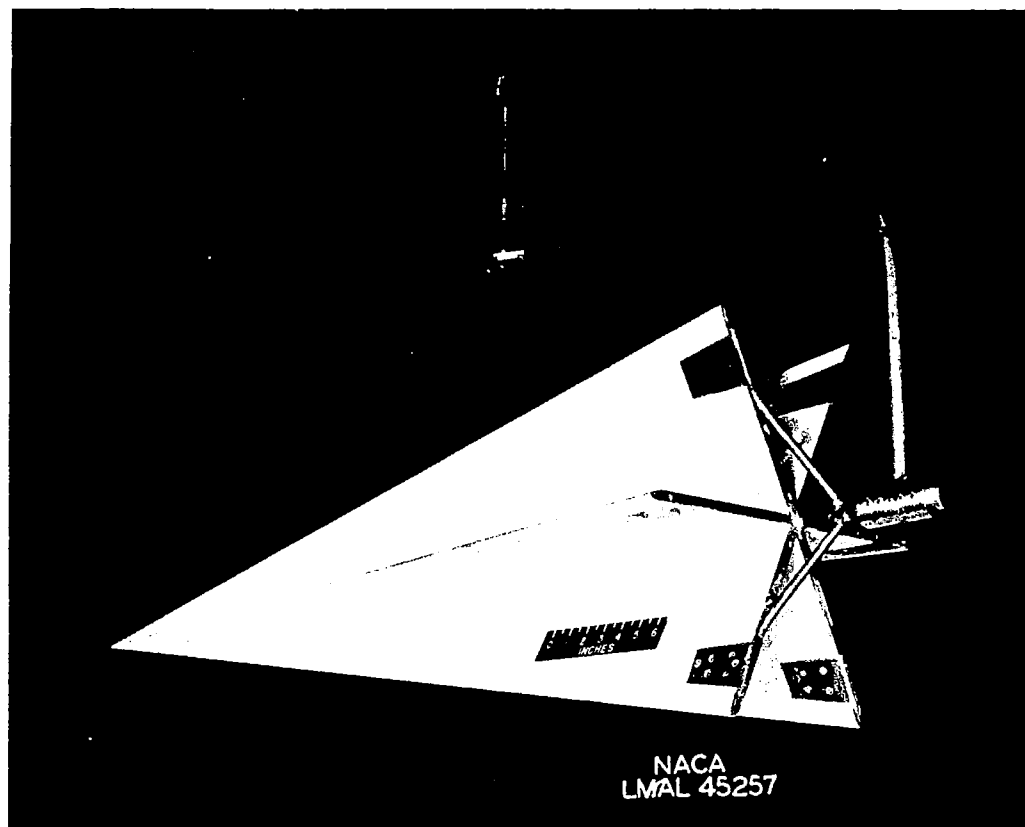
(a) $\phi = 0^{\circ}$.

Figure 3.- Model of six-unit wing design of low aspect
ratio and triangular plan form for guided missiles
tested in the Langley free-flight tunnel.

NACA
LMAL 45259
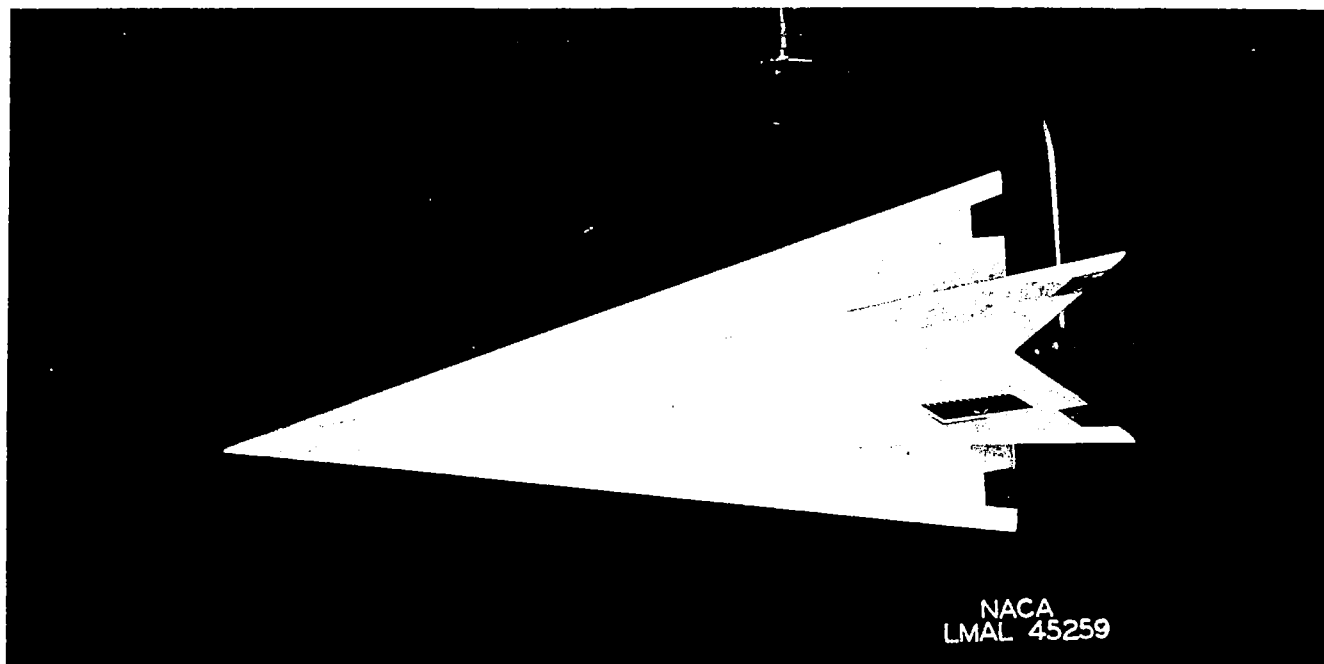
(b) $\phi = 30°$.

Figure 3.- Concluded.
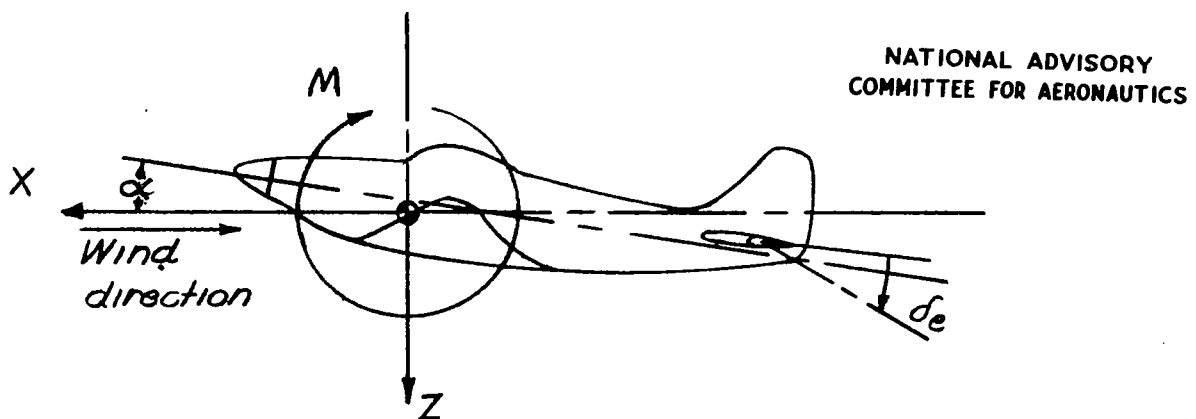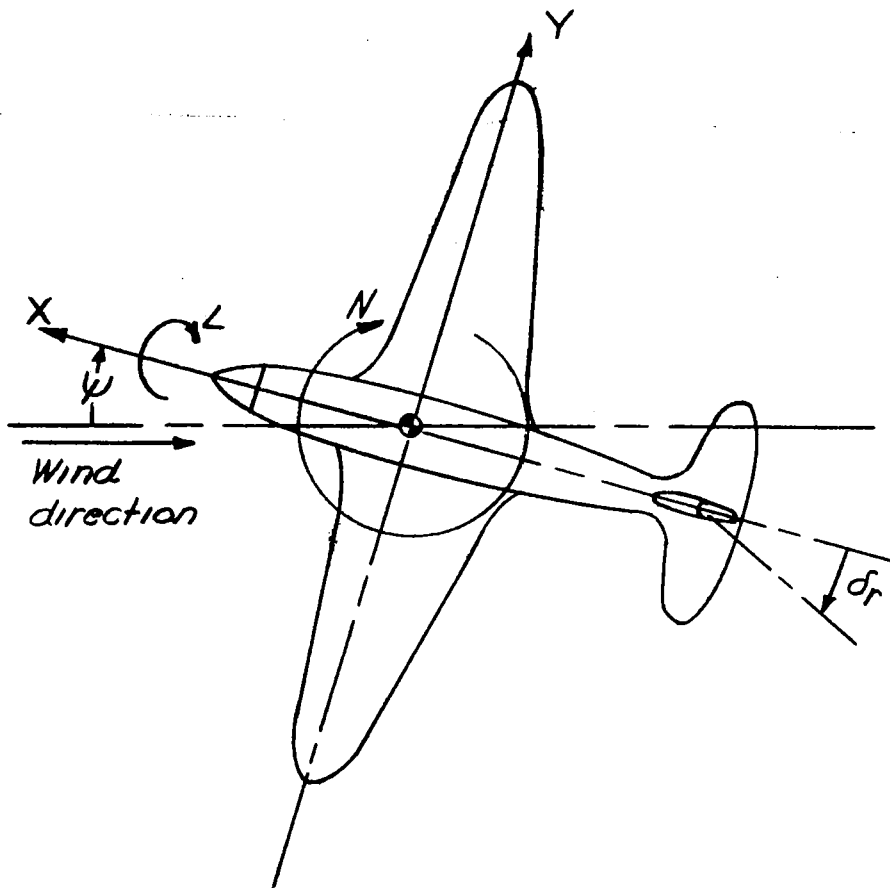
Figure 4.- System of stability axes. Arrows indi-
cate positive directions of moments, forces, and
control-surface deflections.
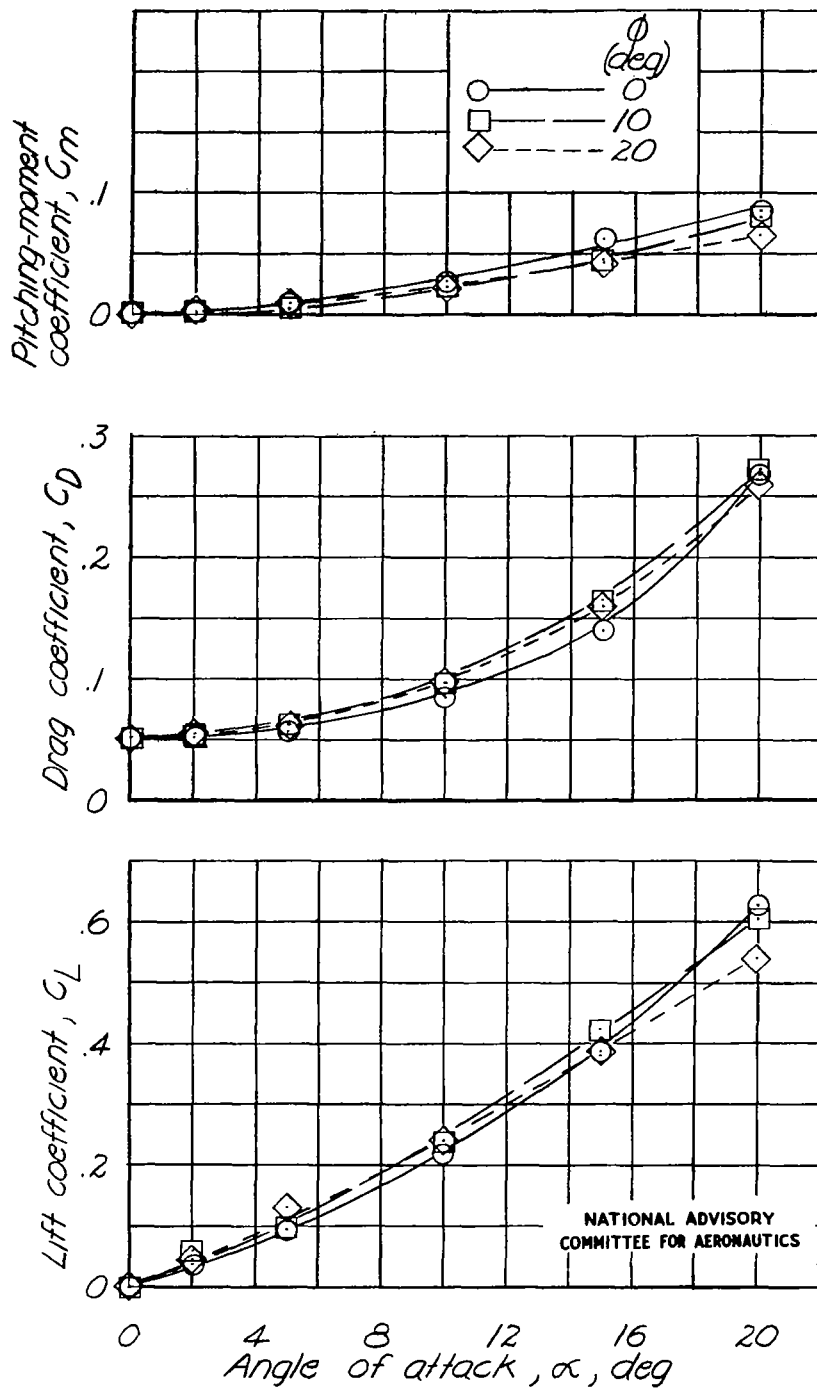
(a) $\phi = 0°, 10°,$ and $20°.$

Figure 5. – Aerodynamic characteristics of four-unit wing design of low aspect ratio and triangular plan form for guided missiles as determined from force tests in the Langley free-flight tunnel. $\psi = 0°$; $q = 4.1$ pounds per square foot.
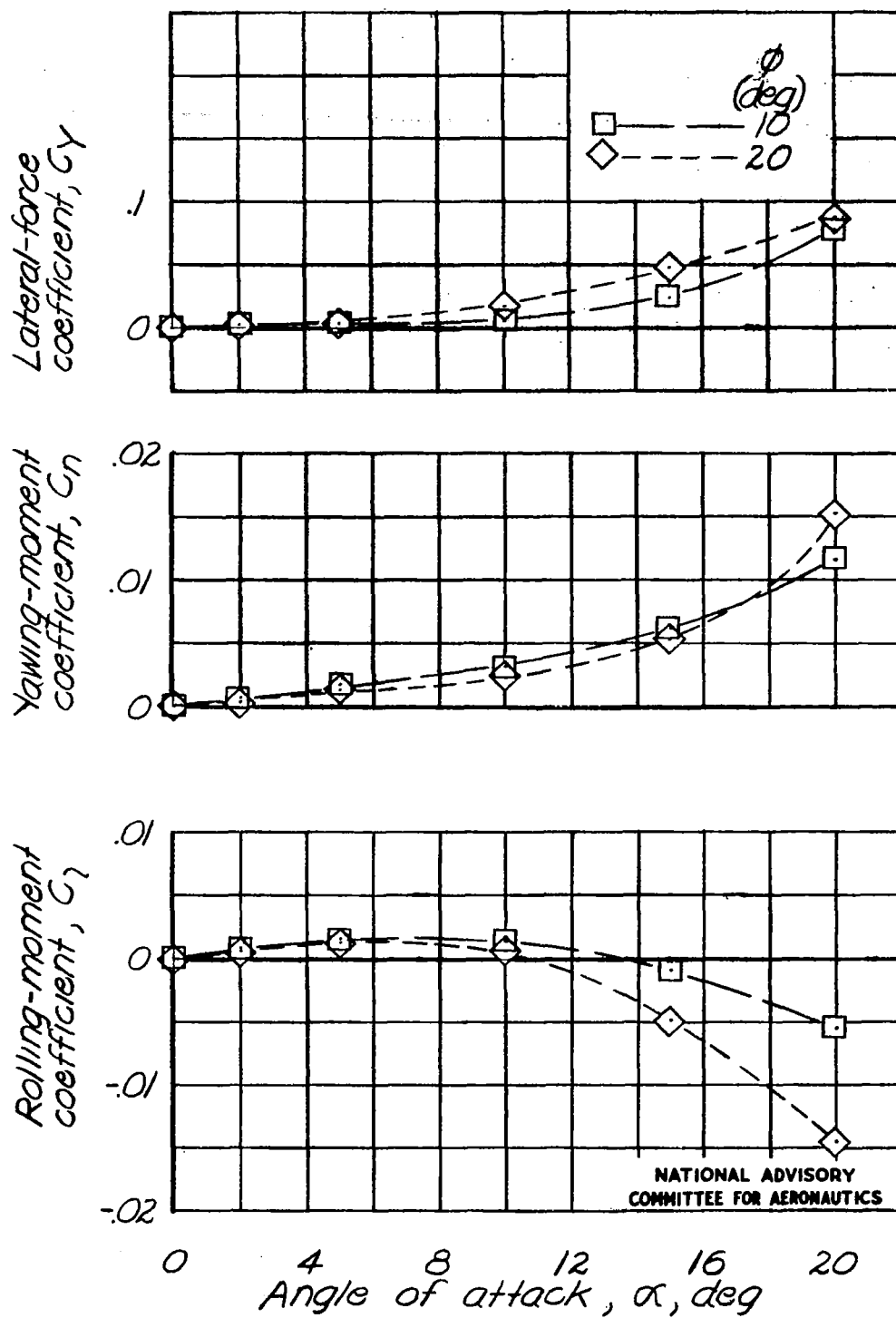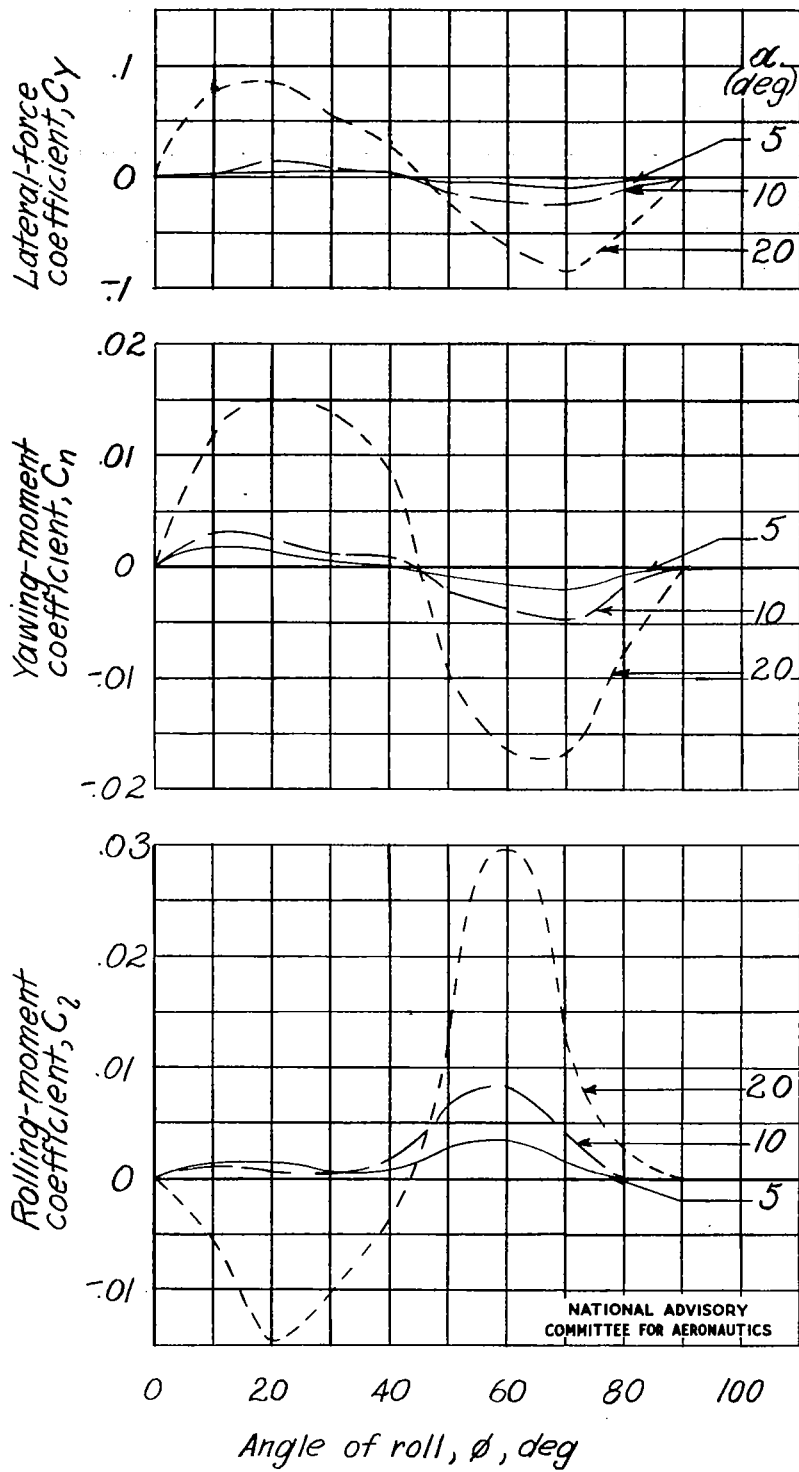
(a) Concluded.
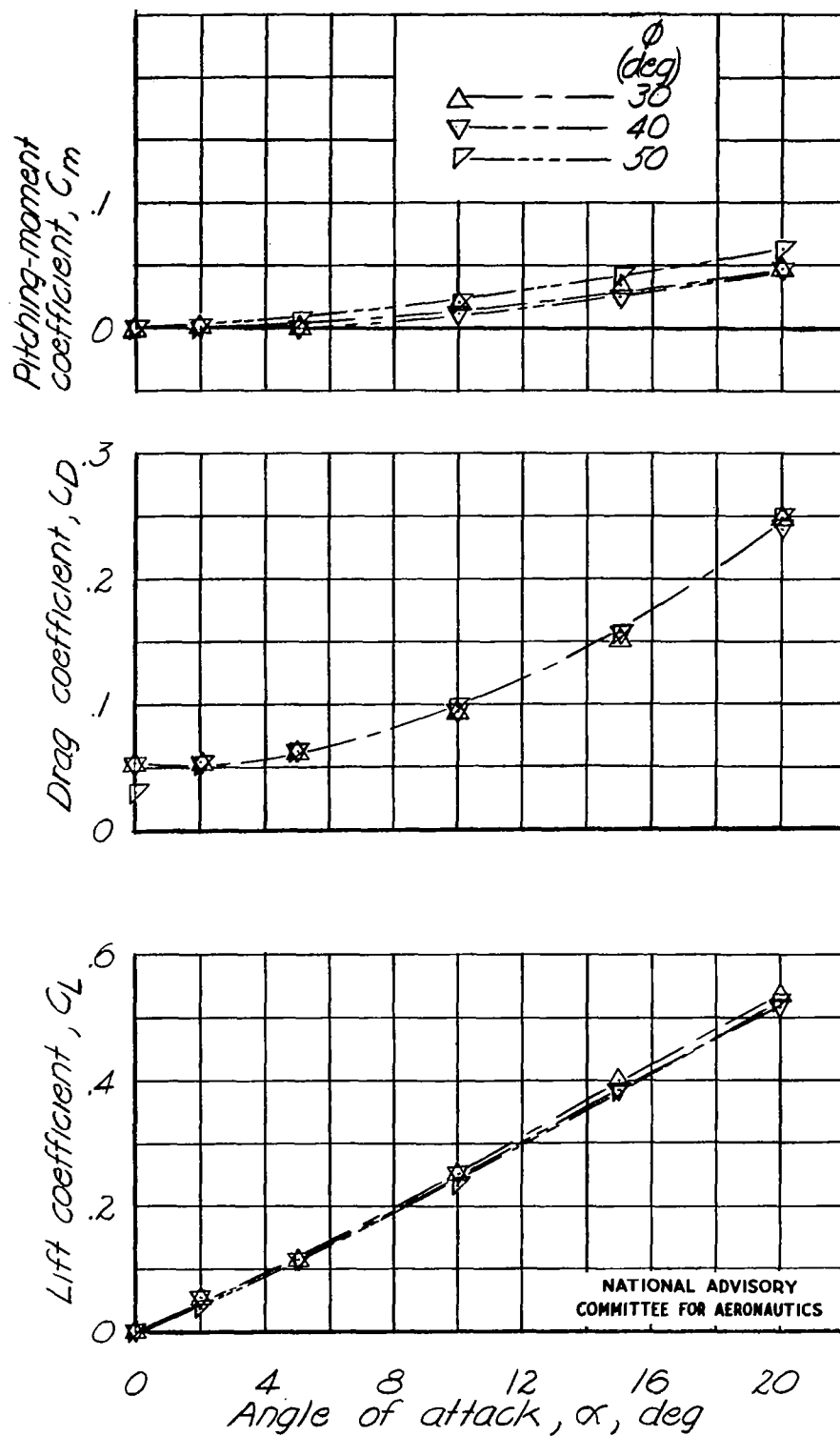
Figure 5.— Continued.

(b) $\phi = 30°, 40°,$ and $50°$.

Figure 5.- Continued.
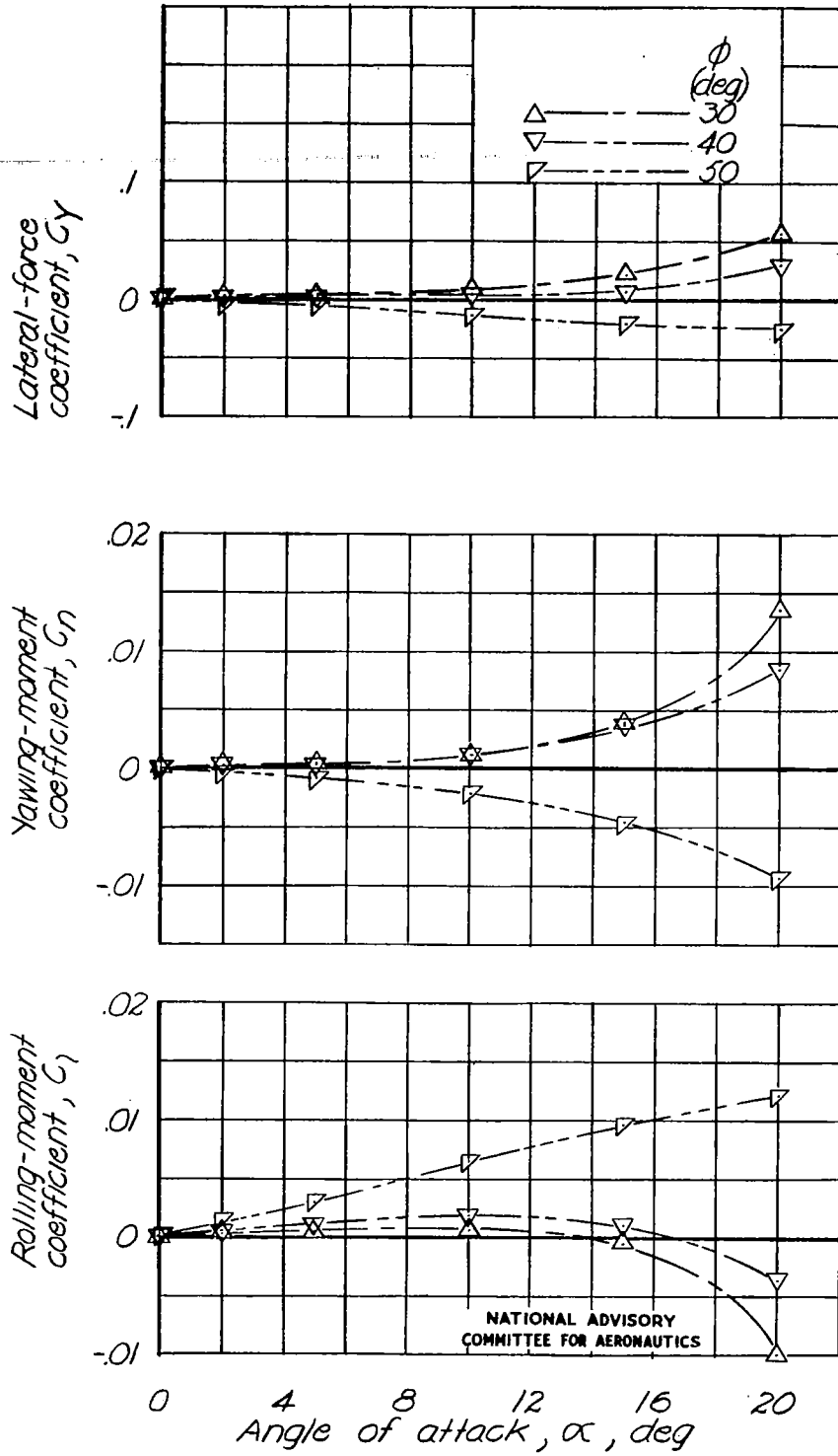
(b) Concluded.
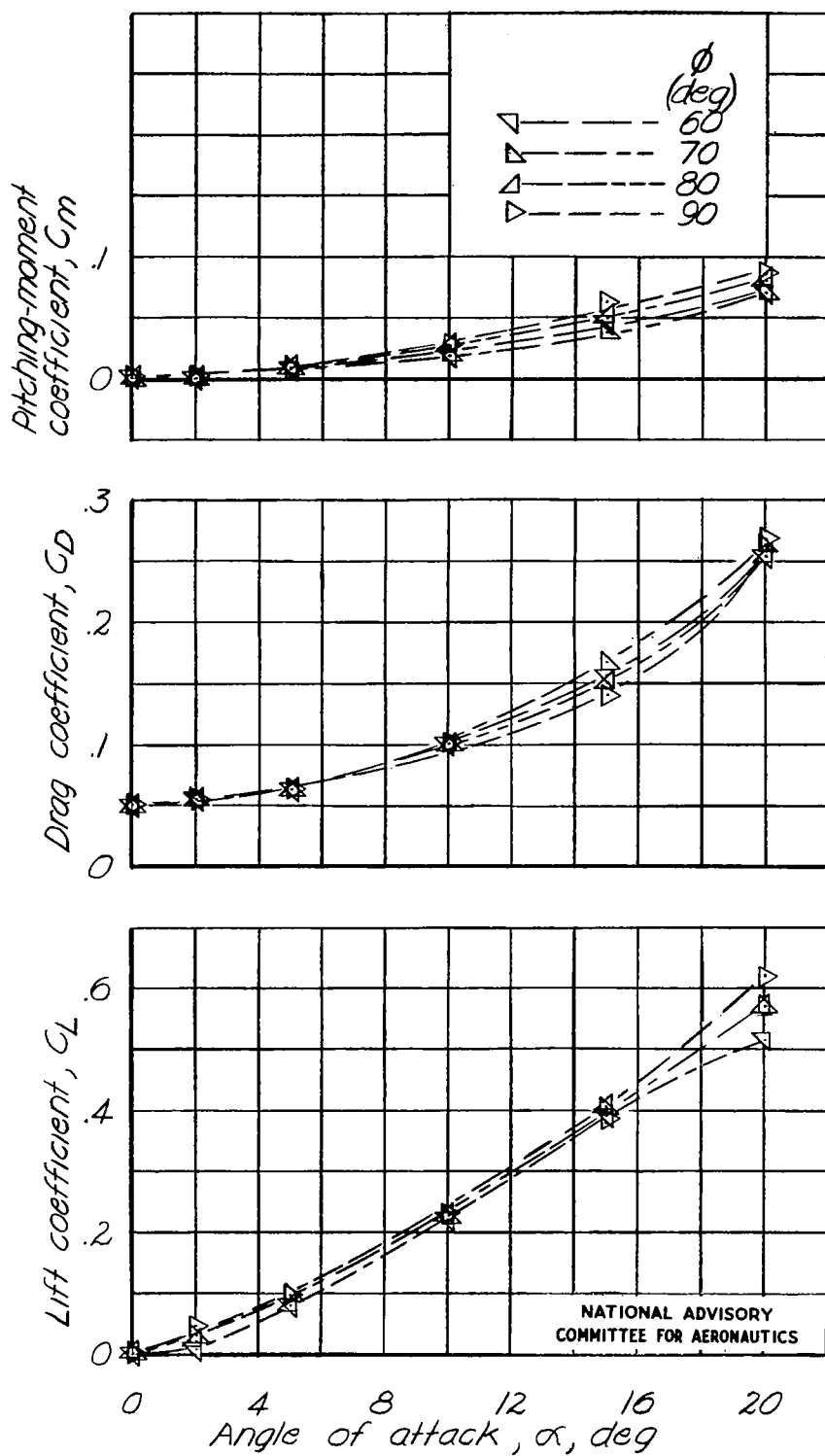
Figure 5.-Continued.

(c) $\phi = 60°, 70°, 80°,$ and $90°.$

Figure 5.- Continued.
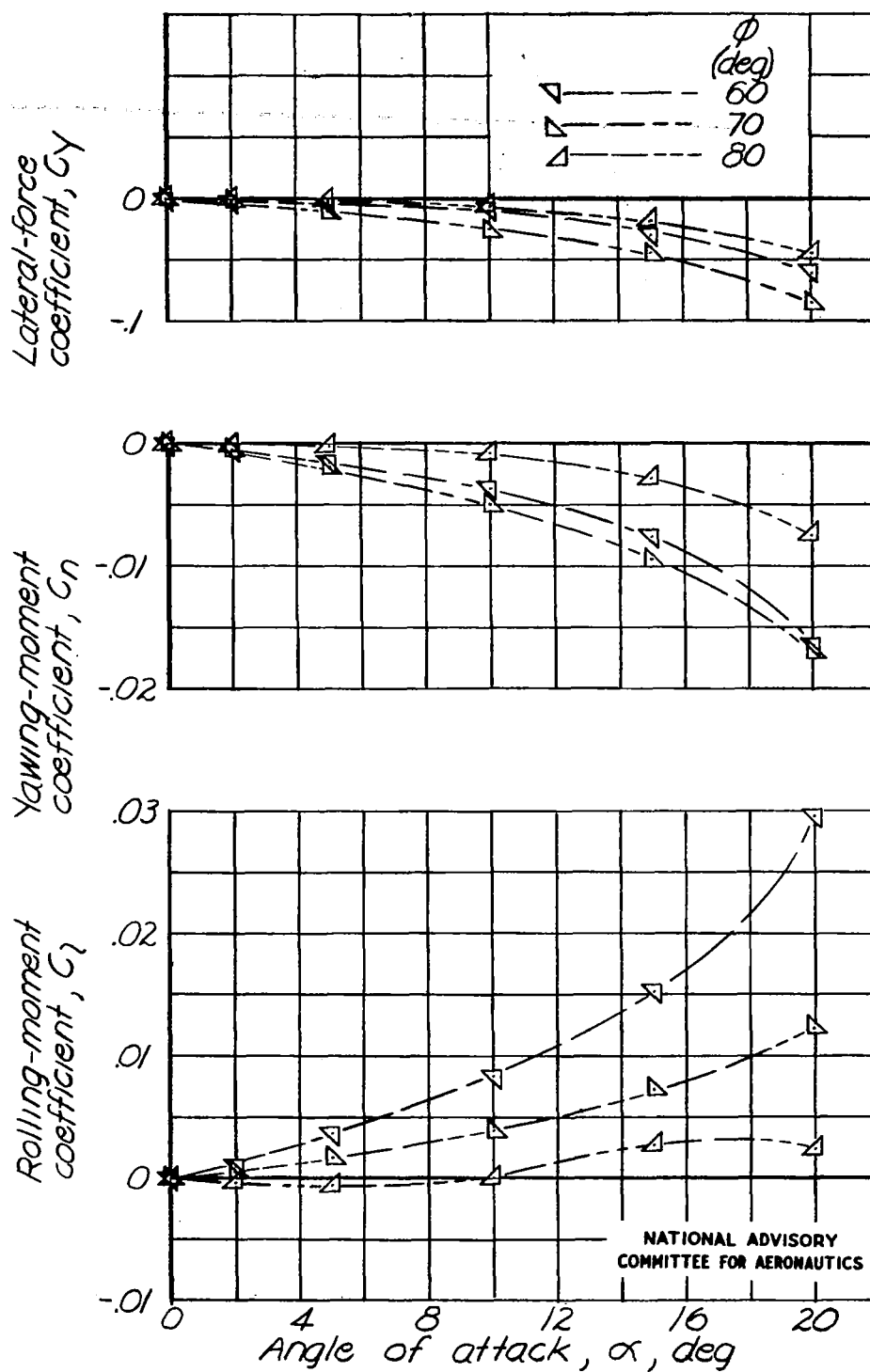
(c) Concluded.

Figure 5.—Concluded.

Fig. 6   NACA ACR No. L6D17a
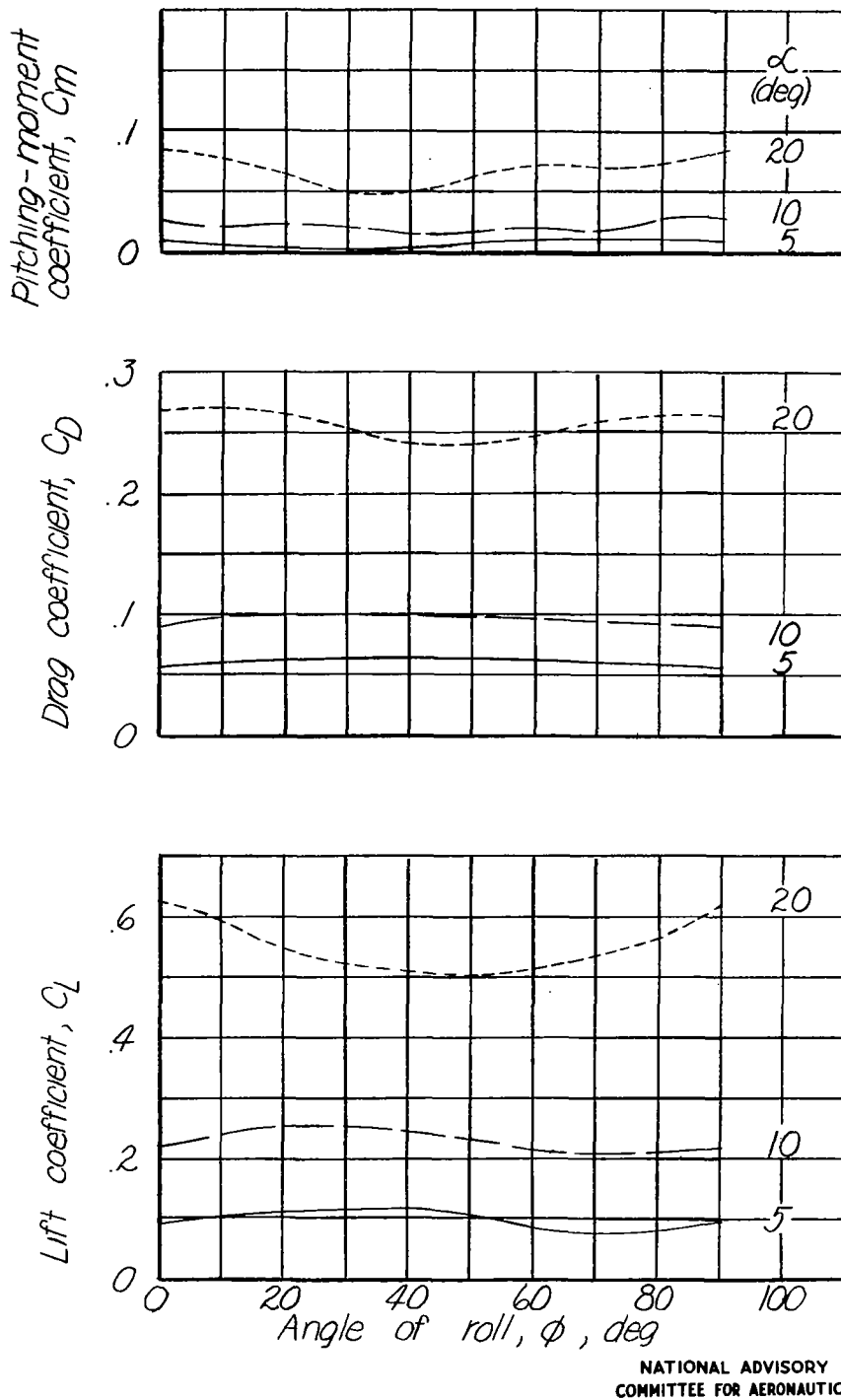
Figure 6.- Variation of aerodynamic characteristics with angle of roll for four-unit wing design of low aspect ratio and triangular plan form for guided missiles as determined from force tests in the Langley free-flight tunnel. $\psi = 0°$; $q = 4.1$ pounds per square foot.

Figure 6.— Concluded.

Fig. 7   NACA ACR No. L6D17a
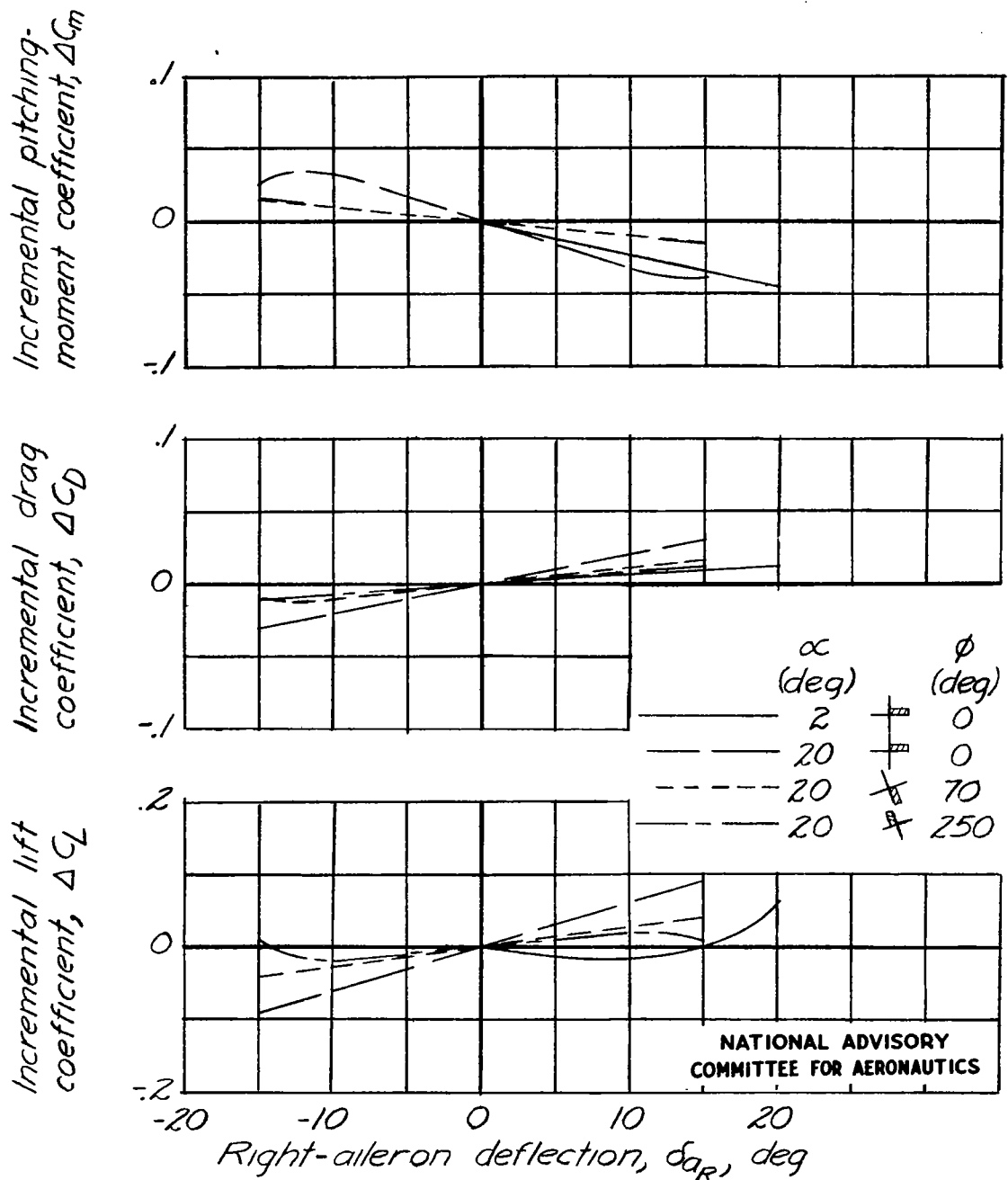
Figure 7.- Control effectiveness of four-unit wing design of low aspect ratio and triangular plan form for guided missiles as determined from force tests in the Langley free-flight tunnel. $\psi = 0°$; $q = 4.1$ pounds per square foot. Control surface on one of four wings; sketches show control positions and negative deflection.
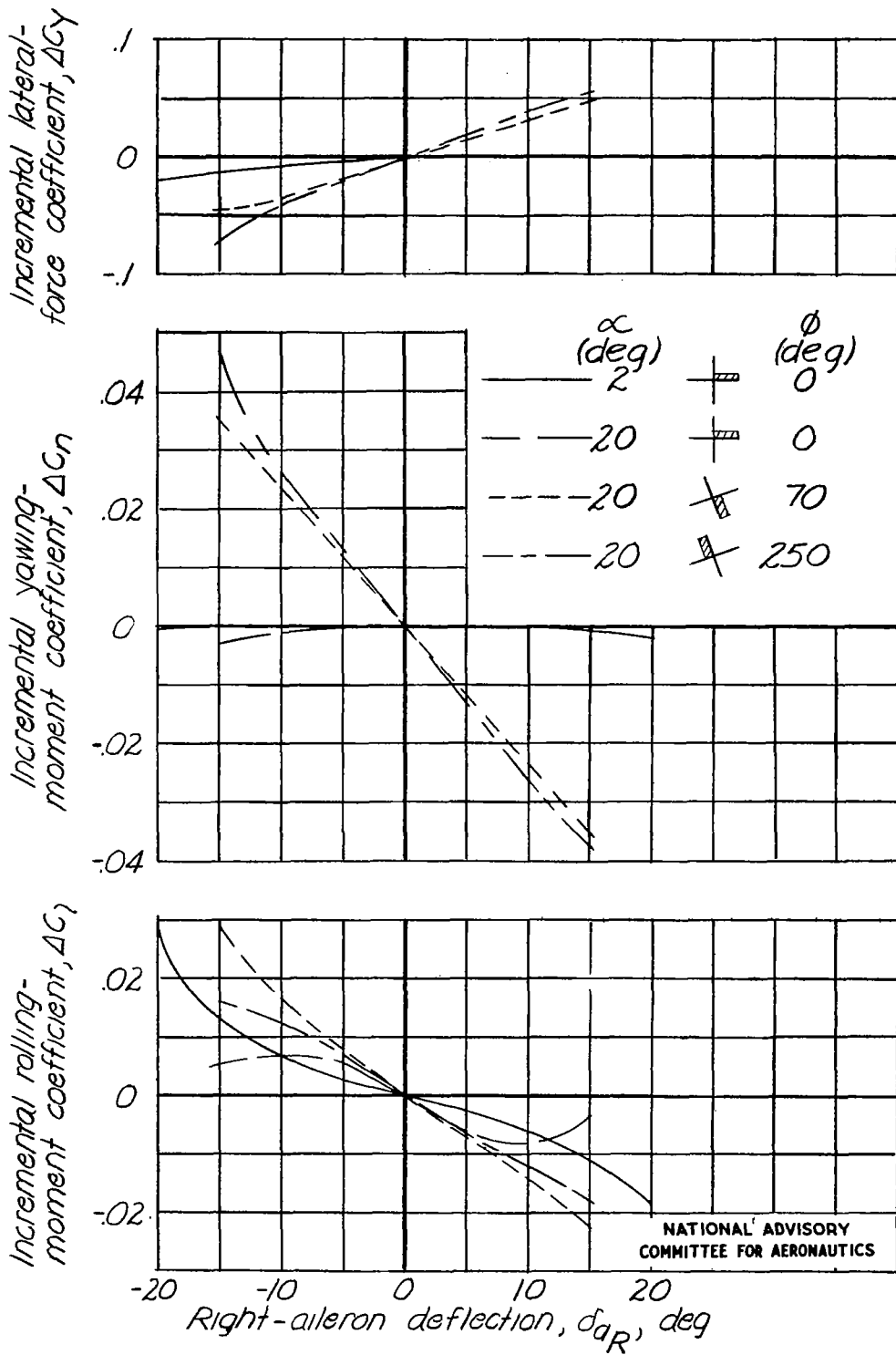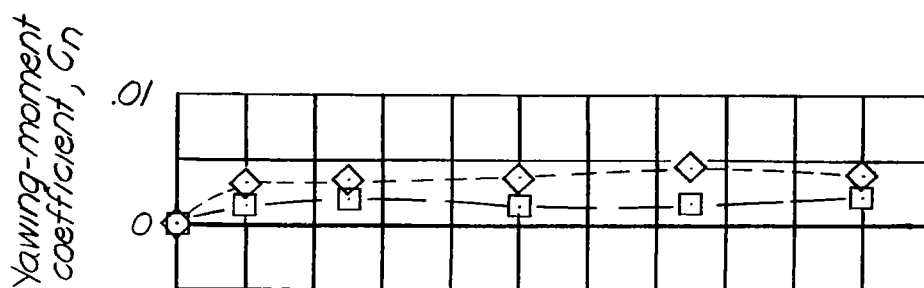
Figure 7.— Concluded.
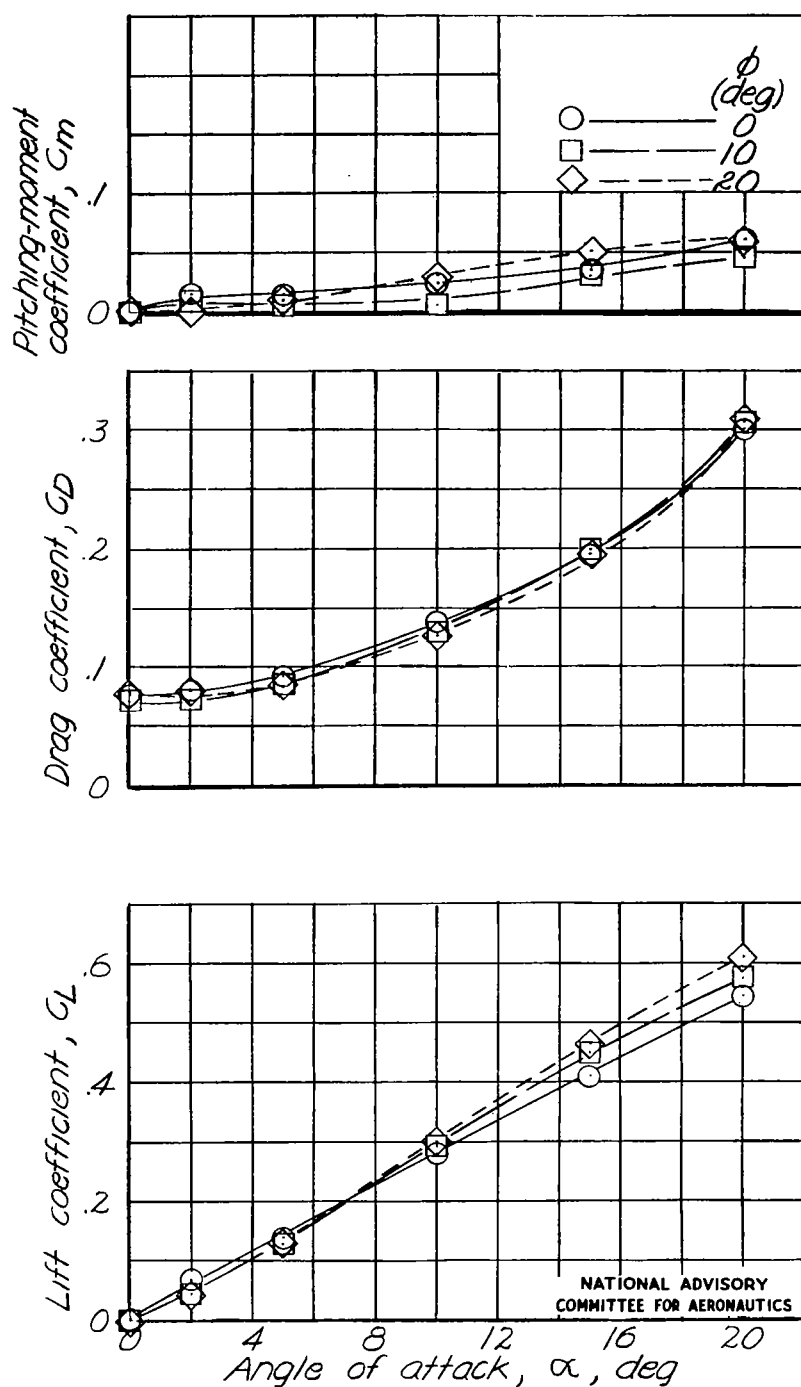
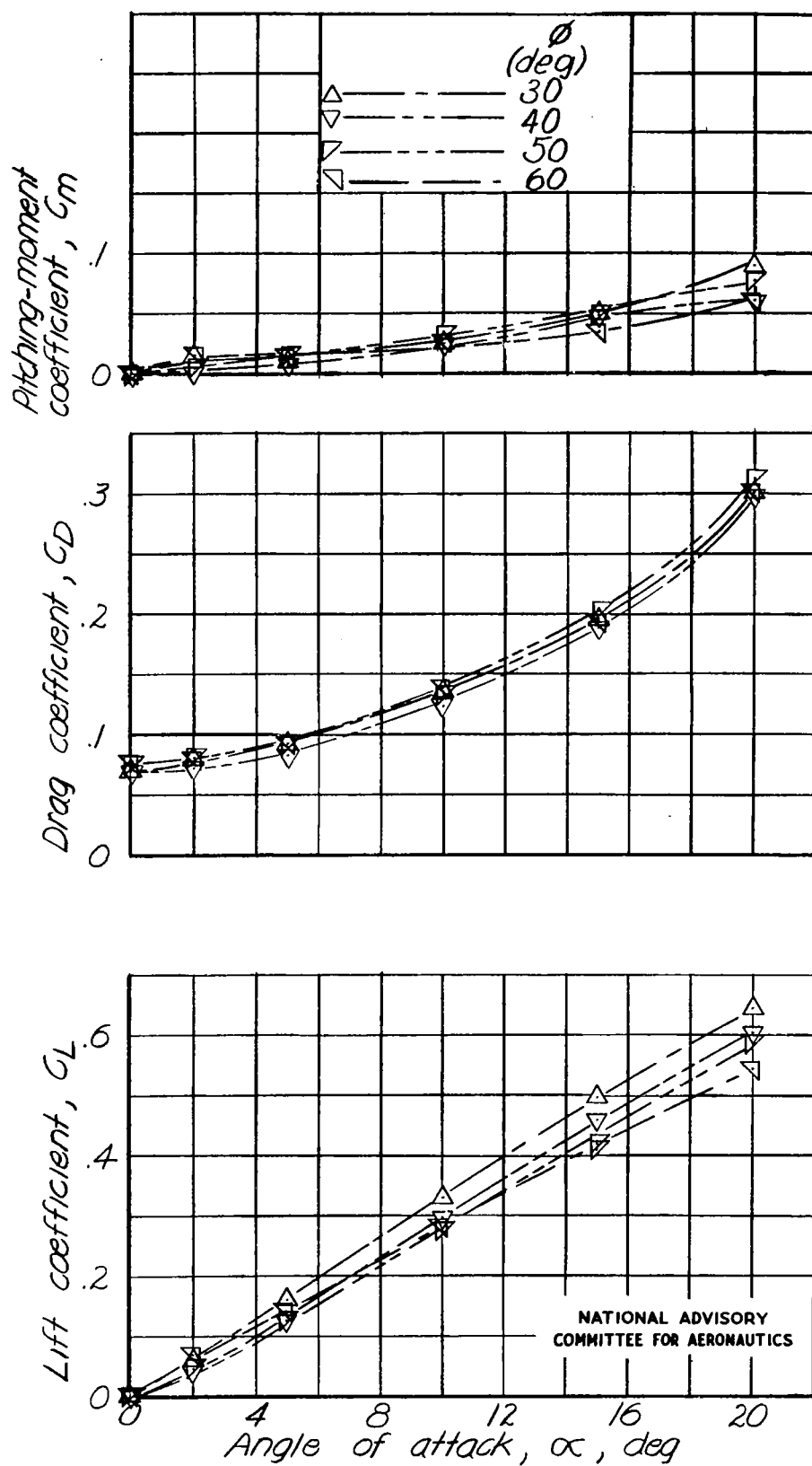(a) $\phi = 0°, 10°,$ and $20°$.

Figure 8._ Aerodynamic characteristics of six-unit wing design of low aspect ratio and triangular plan form for guided missiles as determined from force tests in the Langley free-flight tunnel. $\psi = 0°$; $q = 4.1$ pounds per square foot.
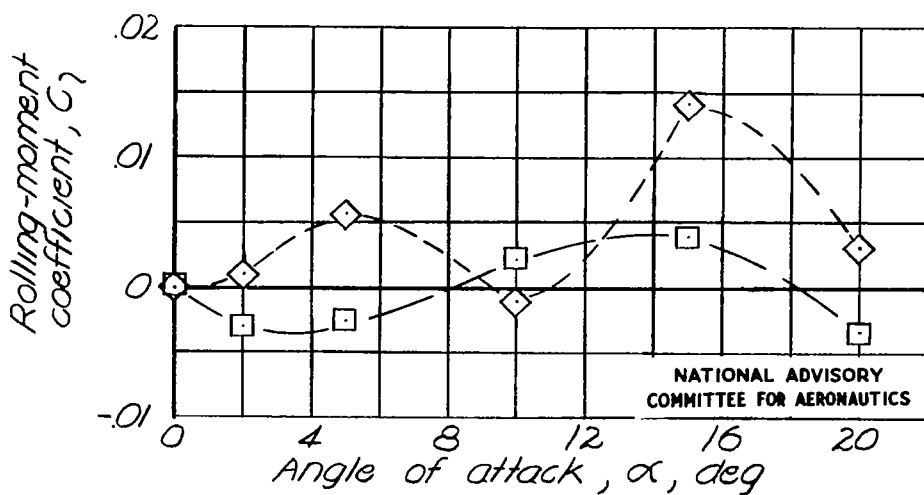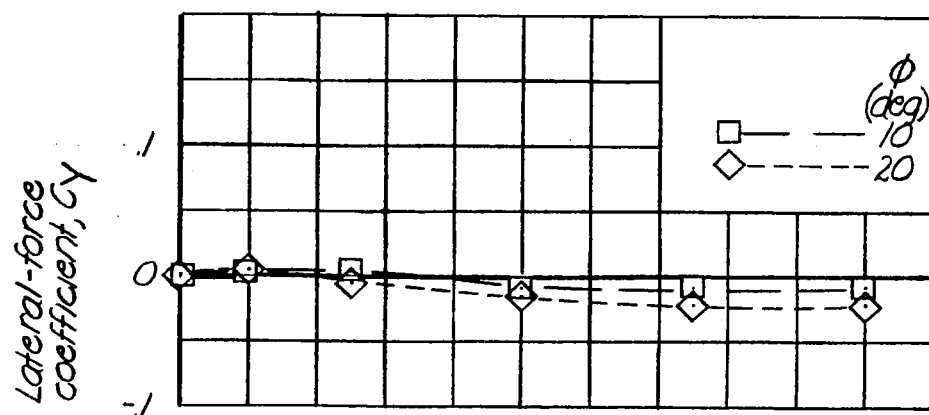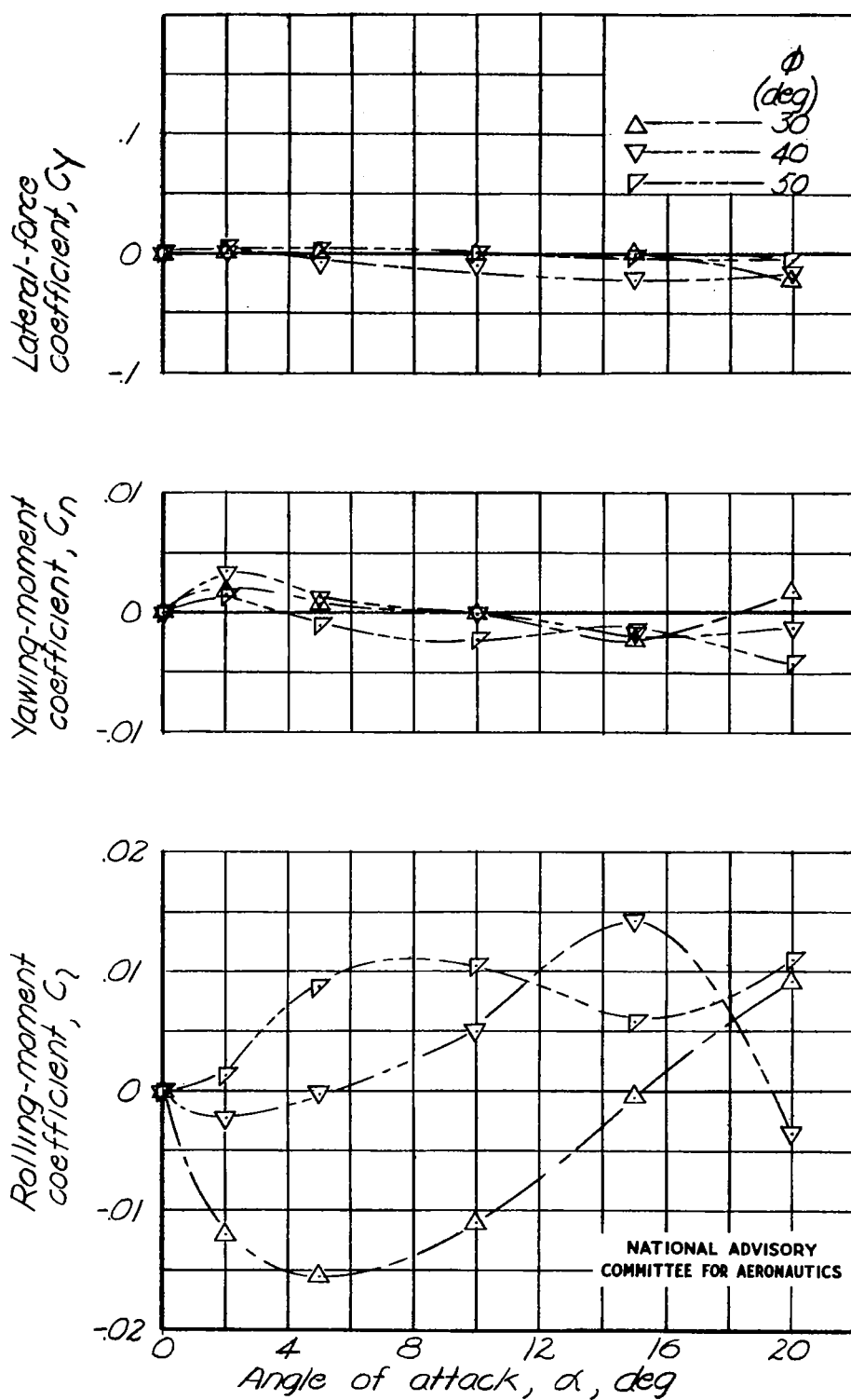
(a) Concluded.

Figure 8.- Continued.

(b) $\phi = 30°, 40°, 50°,$ and $60°$.

Figure 8.- Continued.

(b) Concluded.

Figure 8.- Concluded.

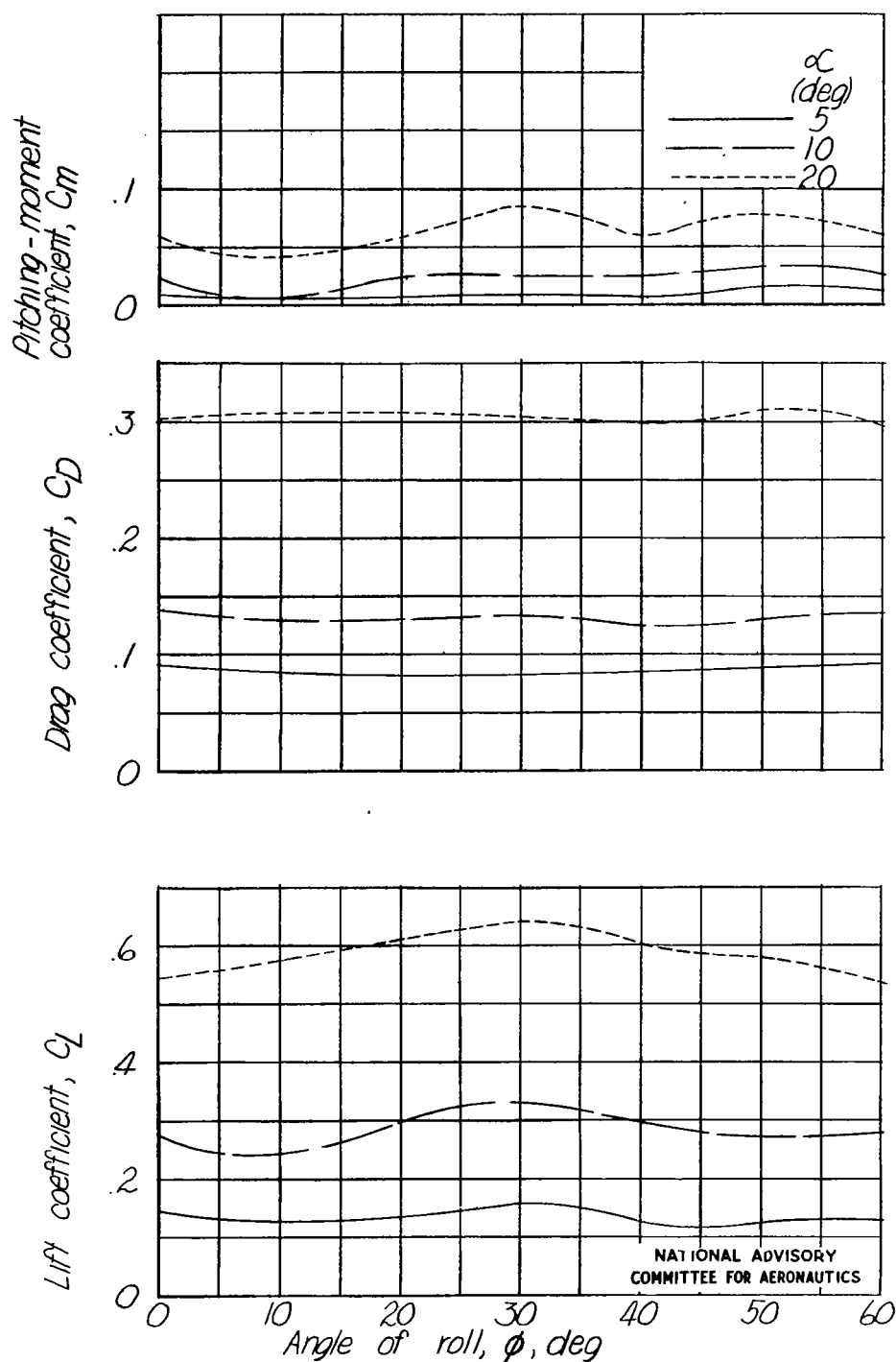Fig. 9   NACA ACR No. L6D17a

Figure 9.—Variation of aerodynamic characteristics with angle of roll for six-unit wing design of low aspect ratio and triangular plan form for guided missiles as determined from force tests in the Langley free-flight tunnel. $\psi = 0°$; $q = 4.1$ pounds per square foot.
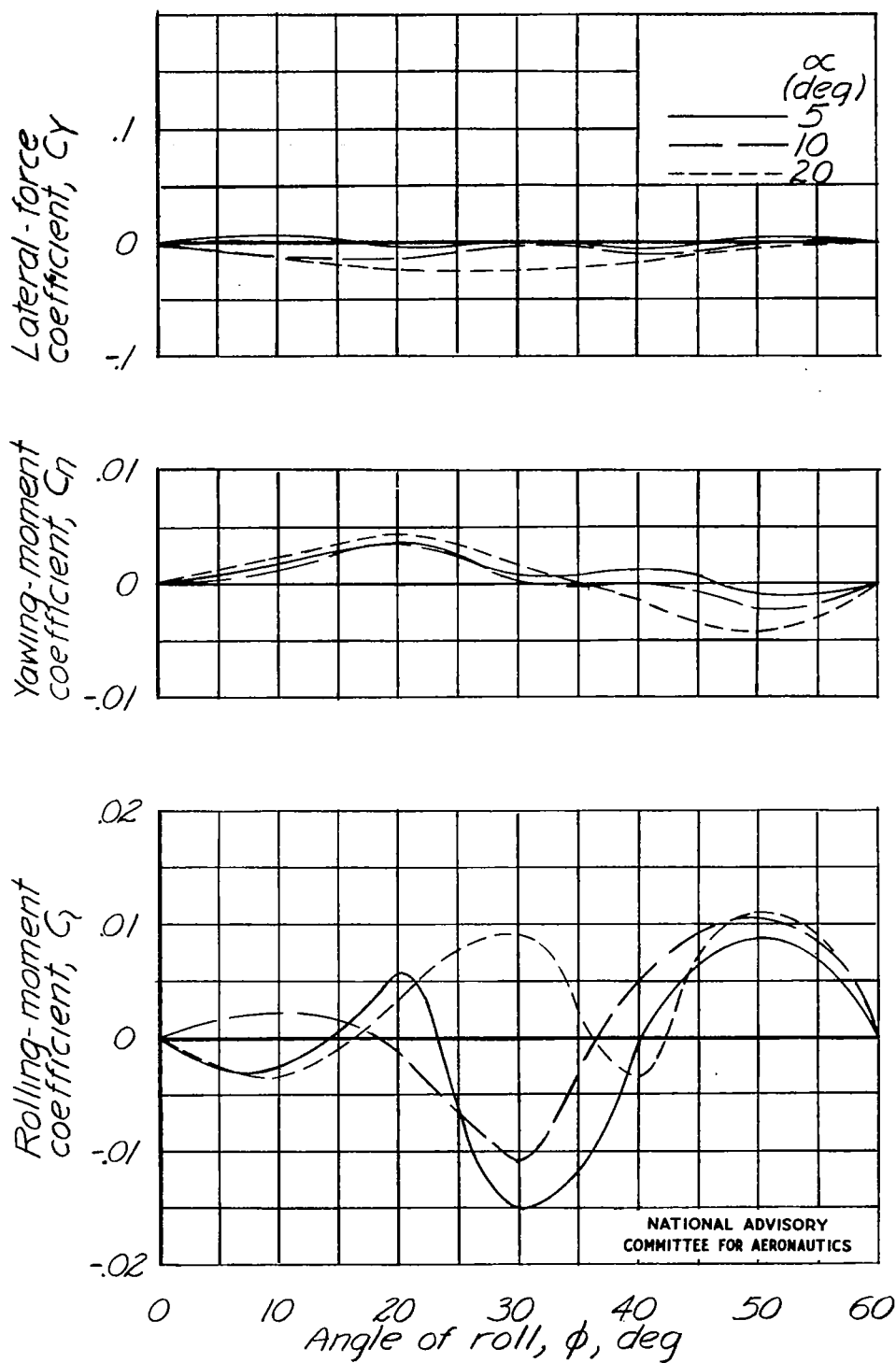
Figure 9.- Concluded.